Connected Vehicles Coordination: A Coalitional Game-Theory Approach

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Abstract—Collective autonomous vehicles are the next step in Intelligent Transportation Systems (ITS) to optimize the traffic flow and increase road safety. However, the management of collective dense scenarios formed by rapid moving vehicles is not a simple task. Thus, a coordination scheme for connected vehicles is proposed in this paper. The coordination and formation scheme is designed using a joint paradigm. On the one hand, the platoon formation is based on a coalitional game-theory approach. On the other hand, the intra and inter-platoon coordination is controlled using a cooperative communication scheme managing the safety and stability of the platoon. Here we define a utility function-based coalitional game to optimize the traffic flow and manage the platoons. In addition, using the information gathered by the deployed infrastructures, the coalitional game behavior is updated in order to react accordingly to unexpected network events and vehicle actions. The platoon management is coordinated using communication schemes in order to achieve the optimal distance between vehicles and platoons, increasing the traffic flow and stability. In order to validate our theoretical framework, simulations are performed under realistic conditions to determine the positive impact obtained by the proposed cooperative scheme in comparison with different approaches.

I. INTRODUCTION

Autonomous driving is considered to be the next big thing in the upcoming years, hence both industry and academia have already turned their eyes to it [1]. It is the key element for the future of Intelligent Transportation Systems (ITS), and hence all efforts are focused on making this technology feasible. Currently, the main progresses in autonomous driving are concentrated in the area of a single-car traveling without considering its cooperation with the rest of vehicles using technologies, such as LIDAR (Light Detection and Ranging) and high resolution maps. Those technologies can possibly be applied in order to avoid collisions while following a predefined route [2]. This approach has shown the potential of autonomous driving, achieving a great success in terms of the number of accidents per kilometer driven [3], including one collision where the Tesla autopilot was exonerated of any fault [4]. Nonetheless, a single autonomous vehicle will not improve the overall traffic flow [5], since it does not take into consideration the rest of the vehicles on the road for more than merely collision avoidance.

In order to add collective adaptation and autonomy to the vehicular network, different communication protocols have been developed in the last years, enabling vehicle-to-vehicle (V2V) and vehicle-to-infrastructure (V2I) communications and improving the efficiency and safety of vehicular networks. At the present time, LTE-V2X, the proposed technology from 3GPP (3rd Generation Partnership Project) in its Release 14 [6], seems like the perfect candidate to be the standard for the next vehicular networks communication scheme considering its advantages. These advantages are, namely, an already deployed communication infrastructure and a robust MAC layer, designed to fulfill the demanding requirements of vehicular communications, in contrast to the non-guaranteed quality of service (QoS) of the IEEE 802.11p technology [7], [8]. The information collected by these communication schemes allows each vehicle to acquire full awareness of the future intentions of the rest of vehicles in the network. Hence, it is possible to mimic the human behavior for cooperation [9] without the uncertainty of unknown behaviors. The reason behind mimicking human behavior is that we tend to use the smallest amount of energy or the shortest path, which translated into vehicular terms, means a lower fuel or power consumption and an optimal path to destination [10], [11]. The main goal of the ITS is to optimize the vehicle fuel and energy consumption along with the chosen destination path, while at the same time, increase the traffic safety. Thus a simple question arises, is it possible to simultaneously achieve these goals? Many different approaches for vehicle organization have been considered, but platooning demonstrates the best performance in terms of fuel consumption and path optimization [12], [13]. It has been proven in a previous work [14] that using V2V communication schemes for intra and inter-platooning organization not only improves safety of the vehicles composing it, but also optimizes the traffic flow, i.e., minimizes the distance between vehicles while maintaining the stability of the platoon. However, the merging and managing of platoons is still an open issue under these safety conditions. Most of the previous works in platooning focus on highways or simple scenarios without taking into consideration the traffic flow optimization or the intra-platoon management [15]. In this paper, a game-theory approach is proposed to address these problems related to more complex scenarios, using vehicular communication schemes, both V2V and V2I, in order to optimize the three main aspects aforementioned, i.e., road safety, traffic flow and fuel consumption.

Similar to human behavior, game-theory approaches face the problem of selfishness in autonomous systems. Therefore, it is required to motivate the autonomous vehicles to cooperate in
order to optimize the system. A joint global goal is added to the game-theory framework, so that the autonomous vehicles aim for the optimal decision, not only for themselves, but for the general system. Several studies have been conducted using a game-theory approach in order to implement platooning, specially for trucks. However, the inclusion of communication schemes for the intra-platoon management was not considered, and hence, optimal cooperation schemes based on communication with different vehicles were not achieved [16], [17]. Different studies have considered coalition games from diverse perspectives, such as heuristic approaches [18], Markov chains theory [19] or concepts from the economic world [20]. However, in our work the used model is based on the set theory methods introduced in [21]. Following the principles of the development of autonomous systems [22], we focus on the use of utility-based functions, and the characterization of the cooperation of vehicles.

The remainder of this paper is organized as follows. Section II introduces the system model along with the platoon cooperative communication scheme. Section III shows the main contribution of this paper, where the coalitional game-theory approach is defined using mathematical concepts. In Section IV, a realistic simulation is performed to show the improvements in the network using the concepts previously introduced, followed by the conclusion in Section V.

II. SYSTEM MODEL

Let a set of vehicles \( \mathcal{N} = \{n_1, \ldots, n_N\} \) grouped in \( K = \{k_1, \ldots, k_K\} \) platoons under the range of \( B = \{b_1, \ldots, b_B\} \) eNodeBs. Each vehicle \( n_i \in \mathcal{N}, i = \{1, \ldots, N\} \) belongs simultaneously to only one platoon \( k_u \in K, u = \{1, \ldots, K\} \), and each platoon is individually connected to a unique \( b_z \in B, z = \{1, \ldots, B\} \) eNodeB. The vehicles are equipped with two different types of on-board equipment, i.e., short-range sensors in order to sense the environment and the surrounding vehicles, and communication devices which enable the V2V and V2I communication schemes. The communication protocol is based on the recently proposed LTE-V2X standard, included in the LTE Release 14. Following the standard proposed by LTE-V2X, the radio resources are allocated using a semi-persistent scheduling (SPS). Each vehicle has resources reserved persistently until it abandons the infrastructure coverage, and the retransmissions or event-based transmissions are dynamically allocated. In the present proposed system model, the infrastructure (eNodeB) works as a scheduler for the SPS, i.e., the radio resources are allocated based on the information gathered by the infrastructure, exploiting its high communication range.

In order to obtain an optimal traffic flow, the vehicles are organized in platoons\(^1\). This is the most efficient way regarding the number of vehicles per lane/hour, due to the smaller gap between vehicles [23]. It has been confirmed in [14] that due to the addition of a V2V communication scheme, the traffic flow rate can be optimized while the stability of the platoon is not affected. The required intra-platoon distance for vehicles driving at a speed \( v_n[mT] \) at time \( mT \) is \( \Delta D = 0.1s \cdot v_n[mT] \) and the inter-platoon distance is \( \Delta D = 1s \cdot v_n[mT] \) to insure stability and safety, as shown in Fig. 1. The update interval is given by the value \( mT, m \in \mathbb{N} \), defined as the adaptation time. Therefore, if the vehicles are traveling in an urban environment at 50 km h\(^{-1}\), the distance between consecutive vehicles in a platoon is approximately 1.5 m, and the distance between two consecutive platoons is 15 m. It is noteworthy that these values are obtained under the assumption of a perfect mechanical response and no sensor failure. Moreover, the information within the platoon is shared using a V2V protocol as follows:

\[
v_n[mT] = v_n[(m-1)T] + a_n[(m-1)T] \cdot T \quad (1)
\]

\[
v_{n+1}[mT] = v_{n+1}[(m-1)T] + a_{n+1}[(m-1)T] \cdot T \quad (2)
\]

\[
S_n[mT] = S_n[(m-1)T] + (v_{n+1}[(m-1)T] - v_n[(m-1)T]) \cdot T + 0.5 \cdot T^2(a_{n+1}[(m-1)T] - a_n[(m-1)T]) \quad (3)
\]

\[
a_n[mT] = f_{control}(v_n[mT], S_n[mT], a_{n+1}[mT], v_{n+1}[mT], S_{min}, T_g, T) \quad (4)
\]

where \( T \) is defined by the LTE standard as 100 ms, and \( v_n[mT] \) and \( a_n[mT] \) are the velocity and acceleration of the corresponding vehicle, respectively. Moreover, \( S_n[mT] \) is defined as the inter-vehicular gap between two successive vehicles. Eq. 4 shows the input parameters in order to adjust the acceleration, \( a_n[mT] \), for vehicle \( n \), regarding the status of the preceding car, and \( T_g \) is the time gap between vehicles. It is noteworthy, that these values are obtained using the short-range sensors installed in the vehicles.

In the model described in [14], the first vehicle of the platoon is considered as the platoon leader and scheduler. All the vehicles in the platoon drive using a car-following model and the pace is marked by the preceding car. However, in the current proposed model, the infrastructure plays the role of scheduler and not the platoon leader as in [14]. Using the infrastructures in order to regulate the network has several advantages, such as extending the electronic horizon due to its higher altitude, in addition to the exchange of information between infrastructures enabling optimal traffic routing. Grouping vehicles in platoons is the optimal formation not only for the traffic flow rate, but also for the fuel or energy consumption of the vehicles, specially in the case of heavy trucks [13]. In our system model, it is assumed that every autonomous vehicle has a predefined initial position and final destination known by the infrastructure. Hence with the layout

\(^1\) the terms platoon and coalition are interchangeable during the entire paper.
of the road network preloaded in the infrastructure, it is possible to predict the position of each vehicle \( n_i \) at every time. Therefore, the network can be defined by a set of links \( \mathcal{L} \) where \((j, l) \in \mathcal{L}\) is the link between the node \( j \) and the node \( l \). Moreover, the density of vehicles for each link, \( \lambda_{j,l} \), can be predicted and updated accordingly using the information gathered by the infrastructures.

### III. Coalitional Game-Theoretic Approach

From the previous section, we conclude that forming platoons is the most efficient way to organize the vehicle network. Accordingly, we define our problem statement: a coalitional game-theory approach is defined considering the particular properties of our scenario, i.e., physical restrictions, communication among vehicles and fast changing environment, while forming coalitions to optimize the traffic flow. In general, maximizing the individual utility function for each vehicle independently does not provide a global optimization, since the payoff of each player is dependent of the joint actions of the rest of the players. Thus the game can be defined as non-transferable utility (NTU) [24], where the value of a coalition is not longer a single value, but a set of utility function vectors, \( v(k_u) \in \mathbb{R}^K \), depending on the actions of the rest of players. Under these assumptions, a dynamic coalition formation game is defined

**Definition 1: Dynamic Coalition Game**

1) Finite set of players \( \mathcal{N} \) forming \( K = \{k_1, \ldots, k_K\} \) coalitions such that for any collection of disjoint coalitions \( \mathcal{N} = \bigcup_{u=1}^{K} k_u \).
2) Creating coalitions may benefit the players involved, but there are also costs of forming a coalition, hence forming grand coalitions is usually not the optimal decision.
3) Finite set of potential actions \( C \) for each player limited by the road network.
4) The game is defined as dynamic since the actions of the players may bring changes in the strength of the players and to the coalition formation.

The game is defined using the triplet \((\mathcal{N}, v, K)\) where the value of a coalition \( K_u \) is denominated as \( v(k_u) \). Since we are using a formation game, i.e., the network structure and costs to form coalitions play a major role, the value for each coalition has the restriction property [25], and hence, the value \( v(k_u) \) has to be calculated in two steps: i) Consider the set of coalitions \( K \) independent of each other and calculate the value of each one (using the canonical definition) as

\[
\nu(k_u) = \sum_{n_i \in k_u} \phi_{n_i}(\nu)
\]

where \( \phi_{n_i}(\nu) \) is the payoff given to the player \( n_i \) belonging to the coalition \( K_u \) by the Shapley value \( \phi \) which is defined as

\[
\phi_{n_i}(\nu) = \sum_{k_u \subseteq \mathcal{N} \setminus \{n_i\}} \frac{K!(N-K-1)!}{N!} [\nu(k_u \cup \{n_i\}) - \nu(k_u)]
\]

where \( K \) and \( N \) are defined as the cardinal of the coalition \( k_u \) and the set of players \( \mathcal{N} \), respectively. Moreover, in the second step ii) the resulting value of the game \( v(k_u) \) is the \( 1 \times K \) vector of payoff functions constructed by combining all the restricted game values \( (k_u, v(k_u)) \).

Using the proposed scheme, we analyzed the dynamic coalition formation game from bottom to top by means of three different utility functions; individual, coalitional and global as shown in Fig. 2. The first level is the individual utility function \( v(n_i) \) for a player \( n_i \in \mathcal{N} \) which considers the local environment, i.e., its own state vector, and the information shared by the infrastructure. The next level corresponds to the coalitional utility function which motivates the creation of coalitions. This function defines the trade-off between the maximization of the individual utility function and the coalitional utility function of the network. Finally, the global utility function where the players are not individuals, but the coalitions are created by several of them.

**A. Individual Utility Function**

In order to formalize the dynamic coalitional game framework, each vehicle \( n_i \in \mathcal{N} \) has an individual utility function as follows

\[
v_{n_i}[x, mT] = d_{n_i}[x, mT] + \tau_{n_i}[x, mT] + \xi_{n_i}[x, mT]
\]

where \( d_{n_i} \) is the distance from the actual position of the player to destination, \( \tau_{n_i} \) is the travel time from the vehicle position to destination and \( \xi \) is a congestion tax created in order to stimulate the creation of coalitions. In this case, \( \tau_{n_i}[x, mT] \) is linearly related to the density of vehicles. The congestion tax variable for a given position \( x \), \( \xi_{n_i}[x, mT] = \tau_{n_i}[x, mT] \cdot f_{n_i}[q, mT] \) where \( q \) is the number of vehicles using the road at the same time. The congestion tax form can be justified by the idea that in a road with more vehicles, it is more likely to create platoons (which are the optimal way of traveling). However, to avoid a high congestion in a single road path, the variable \( \tau_{n_i}[x, mT] \) is included which penalizes a low speed in the given path. Using both considerations, we achieve that the platoons are created with a high probability without congesting the network.

**B. Coalitional Utility Function**

The main goal of our approach is to create coalitions denoted as \( K \) where the total payoff of this particular organization is greater than other possible set of coalitions \( S \), i.e., \( v(K) > v(S) \). Therefore, in order to motivate the vehicles to join a coalition, and consequently, obtain an optimal management of the traffic, the following concept must be fulfilled:

\[
v(k_u) \geq \sum_{i=1}^{N} v(n_i^{k_u})
\]

this concept follows the Pareto order which states that a player \( n_i^{k_u} \in \mathcal{N} \) belonging to a platoon \( k_u \) will prefer to join the coalition \( k_u \) if at least one player belonging to \( k_u \) improves its utility function without hurting any of the other players.
Hence, if Eq. 8 is fulfilled no individual vehicle would have the incentive to abandon the coalition since the individual utility function outside a coalition is always smaller, or at best equal, compared to the coalitional utility function. Therefore, the optimization problem for the coalitional utility function is defined as follows

$$\min_{d_n, [x, mT], \tau_n, [x, mT], \xi_n, [x, mT]} \nu(k_u) = \sum_{i=1}^{N} \hat{\nu}(n_i)$$  \hspace{1cm} (9a)

s.t.  \hspace{1cm} \hat{\nu}_n[x, mT] = \hat{d}_n[x, mT] + \hat{\tau}_n[x, mT] + \hat{\xi}_n[x, mT]$$  \hspace{1cm} (9b)

The value $\hat{\nu}(n_i)$ is defined using the optimal values for the coalition $k_u$ which satisfies Eq. 8 and fulfills the condition $\nu(K) > \nu(S)$, however, they do not need to be the optimal for the individual payoff function $\nu(n_i)$. It is important to mention that the coalitional utility function, $\nu(k_u)$ denoted in Eq. 9a, should be fair for each vehicle $n_i \in k_u$, i.e., no vehicle should be left starving which in game-theory is denoted as $\hat{\nu}(n_i) \to \infty$. In order to update the cost parameters $d_n, [x, mT], \tau_n, [x, mT], \xi_n, [x, mT]$, the infrastructure requires the following information:

- State vector for each vehicle $n_i \in \mathcal{N}$
  
  $\hat{S}V_n := (p_n, mT, v_n, mT, h_n, mT)$.

- Initial and desired final position $(\hat{f}_0, \hat{f}_1)$ for each vehicle $n_i$

- Road network information and cost coefficients $\beta_{j,i}[mT], \gamma_{j,i}[mT]$ for each path.

Moreover, each individual vehicle in this scenario is also able to take evasive and safety decisions on its own and without the assistance of the infrastructure, as a way to improve the safety against disconnections, following the principles of implicit coordination [26].

C. Global Utility Function

Once the coalitions are formed and the coalitional function is maximized, we proceed in a way where the global utility function is enhanced by the centralized architecture. In practice, due to the communication limitations, in both range and reliability, the number of members for each platoon is limited. In order to obtain an optimal system where all the different coalitions help to maximize the general utility function, the cost coefficients $\beta_{j,i}[mT]$ and $\gamma_{j,i}[mT]$ are estimated using the infrastructure. These parameters provide external information to the players in order to adjust their payoff function. The chosen coefficient will be the one maximizing the general utility function, even if it is not optimal for the individual or coalition utility function. The use of an infrastructure contributes to add global perception to the system, along with the distributed perception of each individual vehicle.

IV. SIMULATION RESULTS

In order to validate the theoretical framework introduced in the previous sections, a realistic simulation is implemented. The simulation is performed considering a road network as depicted in Fig. 3, and its equivalent in graph form as shown in Fig. 4. The graph-form network is formed by the nodes (roadway points), and the weights of the edges connecting these nodes. The vehicles are generated using a Poisson distribution, and the initial and final node of each vehicle are chosen randomly from the entire set of nodes. The communication scheme parameters for the simulation are shown in Table I.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Frequency</td>
<td>5.9 GHz</td>
</tr>
<tr>
<td>Transmission Power</td>
<td>23 dBm</td>
</tr>
<tr>
<td>Max. Vehicle Speed</td>
<td>90 km h⁻¹</td>
</tr>
<tr>
<td>Number of vehicles</td>
<td>40</td>
</tr>
</tbody>
</table>

For the simulation parameters, the values presented in Table I were considered to be the standard values used in vehicular communications. In order to obtain a realistic simulation, we have also taken into consideration the limitations of the road network and the communication scheme as analyzed in
Section II. The proposed model is compared with two different approaches. The first one is the simplest routing algorithm, based on the shortest path, with no incentives to create platoons, and no inter-vehicular communication to optimize the traffic flow. The second approach is published in [17], which includes an incentive for a certain number of trucks in order to form platoons. This scheme has no centralized architecture, and additionally, does not optimize the traffic flow by means of minimizing the inter-vehicular distance. The goal of our game-theoretical approach is to motivate the creation of platoons, hence we aim to route most of the vehicles by the same routes to motive the creation of coalitions, nevertheless avoiding extreme congestion. Additionally, the second goal is to minimize the time to destination of the vehicles, i.e., use the platoon formations and the global perception to detect the fastest routes for the particular vehicles. Therefore, the first parameter to analyze is the load per path, and additionally compare it with the other two approaches as shown in Fig. 5.

<table>
<thead>
<tr>
<th></th>
<th>Mean</th>
<th>Std. Dev. (SD)</th>
</tr>
</thead>
<tbody>
<tr>
<td>No Incentive Scheme</td>
<td>31.7724</td>
<td>8.3413</td>
</tr>
<tr>
<td>Truck Incentive Scheme [17]</td>
<td>28.5292</td>
<td>10.8876</td>
</tr>
<tr>
<td>Proposed Incentive Scheme</td>
<td>25.8265</td>
<td>10.3222</td>
</tr>
</tbody>
</table>

The simulation results show a lower mean load per path (see Table II) in our scheme compared to the other two, which results in a minimization of the overall network costs. Moreover, in comparison with the no incentive scheme, the standard deviation is higher indicating the incentive to drive in some paths over others in order to create platoons. Regarding the scheme proposed in [17], the mean load per path is higher than in our case, due to the lack of an inter-platoon optimization scheme, and that not every vehicle has the equipment to form coalitions. Moreover, the statistical analysis, in Table II, shows the improvement in network costs obtained by means of the infrastructure.

The second parameter under consideration is the mean travel time to destination for the vehicles as shown in Fig. 6. The goal of this parameter is evident, minimize the average time to destination for the vehicles. The statistical analysis shown in Table III presents that our proposed scheme outperforms both the no incentive scheme and the one proposed in [17]. It is noteworthy to mention that our scheme achieves the best results not only in average time travel to destination, but also with the smallest standard deviation which is the indicator of a fair game, i.e., no vehicle is left starving. Furthermore, this parameter shows that introducing incentives in the network, in order to form platoons, improves the overall network performance in terms of average time to destination.

Fig. 3: Roadmap for the simulation example.

Fig. 4: Graph form of the network including the weights for each edge.

Fig. 5: Load for each path comparing the three schemes.
In this paper, we propose a coalitional game-theory approach designed to offer incite the formation of platoons under realistic communication constraints. Once the platoons are created, the management and safety conditions are handled by V2V and V2I communication schemes. It has been demonstrated that the best way to optimize the traffic flow and safety is prioritizing the creation of platoons, which are optimized under a global coalitional game. The overall performance of the network is improved in terms of traffic efficiency and network load, although it may go to the detriment of individual utility functions. The main contribution of this work is to establish a theoretical framework which incites the creation of platoons, and consequently increase the safety and traffic throughput, while showing an improved network performance.

**TABLE III: Statistical Analysis for trip time to destination**

<table>
<thead>
<tr>
<th>Scheme</th>
<th>Mean [s]</th>
<th>Std. Dev. (SD)</th>
</tr>
</thead>
<tbody>
<tr>
<td>No Incentive Scheme</td>
<td>60.5190</td>
<td>32.2363</td>
</tr>
<tr>
<td>Truck Incentive Scheme [17]</td>
<td>54.5467</td>
<td>29.7144</td>
</tr>
<tr>
<td>Proposed Incentive Scheme</td>
<td>40.0651</td>
<td>19.0869</td>
</tr>
</tbody>
</table>

**V. CONCLUSION**

In this paper, we propose a coalitional game-theory approach designed to offer incite the formation of platoons under realistic communication constraints. Once the platoons are created, the management and safety conditions are handled by V2V and V2I communication schemes. It has been demonstrated that the best way to optimize the traffic flow and safety is prioritizing the creation of platoons, which are optimized under a global coalitional game. The overall performance of the network is improved in terms of traffic efficiency and network load, although it may go to the detriment of individual utility functions. The main contribution of this work is to establish a theoretical framework which incites the creation of platoons, and consequently increase the safety and traffic throughput, while showing an improved network performance.

**REFERENCES**


[4] U.S. Department of Transportation, National Highway Traffic Administration, “The automatic emergency braking (aeb) or autopilot systems may not function as designed, increasing the risk of a crash,” 2016.


